Report No. NADC-90001-60





PREDICTION OF FIBER/MATRIX INTERPHASE PROPERTIES AND THEIR INFLUENCE ON INTERFACE STRESS, DISPLACEMENT AND FRACTURE TOUGHNESS OF COMPOSITE MATERIAL

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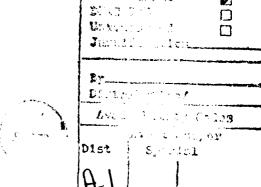
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INTRODUCTION

The fiber/matrix interface has a significant influence on the structural integrity of a fibrous composite. For example, the stronger the interface bond, the higher the composite's static strength. However, a strong interface bond also yields a brittle and notch-sensitive composite² and, on the other hand, a weaker interface results in a higher fracture toughness composite.^{2,3}

Conventional methods for predicting the stress at the fiber/matrix interface can be divided into three categories. These are: shear lag theory, 4,5,8 two-dimensional, finite-element analysis, 7,8 and three-dimensional, finite-element analysis. These methods all assume zero interface thickness and uniform, homogeneous matrix properties.

Recently, several researchers have suggested that the volume of material immediately surrounding the fiber is significantly different from the bulk matrix. 10,11,12,13 This volume of material is commonly referred to as the interphase. Drzal 10 has suggested that this material may be more rigid than the bulk matrix. Piggott 11 has found that to explain the Young's moduli of short-fiber composites, the interphase must have a very low modulus, i.e., much softer than the bulk matrix.

No direct evidence has been found for the presence of an interphase in organic matrix composites nor are its properties and dimensions known. The objective of this study is to prove the existence of interphase and to determine interphase elastic properties, if possible. Included in this work is an investigation to determine the influence of interphases on stress at the fiber/matrix interfaces on displacements and on fracture toughnesses of fibrous composites.

SHEAR LAG THEORY WITH DISTINCT INTERPHASE

To include the interphase into a composite-material structural analysis model, material properties and the thickness of the interphase must be known in advance. Experimental data on interphase properties does not exist. One way to deduce the interphase characteristics is to assume initial values for the interphase and then iterate the properties and thickness until analytical results converge to match the corresponding experimentally observable results.

Since the thickness of interphase can be very small compared with the fiber diameter, a very large number of finite elements would be needed if the finite element technique was used for the iteration procedure. This would be time-consuming and costly. A closed-form solution, based upon shear-lag theory, was employed instead.

In the following, a shear lag analysis, which includes and interphase region between the fiber and bulk matrix, has been developed. Mandell's microdebonding test data was used to determine the interphase material properties and thickness.

THEORY

Mandell's microdebonding test,¹ Figure 1, was modeled as shown in Figure 2. Four types of materials were included in this model; namely, fiber, interphase, matrix, and composite. Note that a load is applied at the end of a fiber, and that the material outside the matrix was modeled as equivalent smeared composite material.

By employing the shear lag theory, the following assumptions were made:

(1) Axial load is carried by the fiber alone, while the interphase and matrix carry the shear load only.

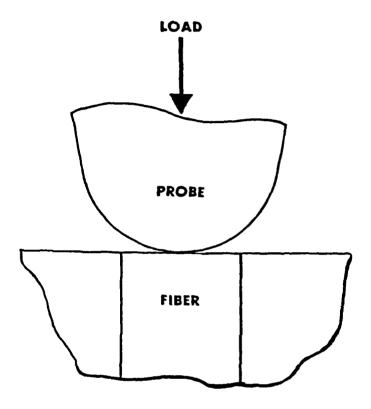


Figure 1. Schematic of Loading for Microdebonding Test.

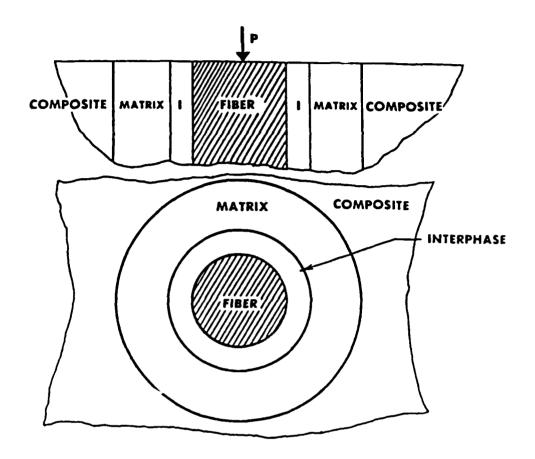


Figure 2. Modeling of Fiber/Matrix Interface.

(2) Fixed boundary conditions apply at the boundary between the matrix and equivalent composite.

The freebody diagrams of the loaded fiber and adjacent interphase and matrix are shown in Figures 3a and 3b. The equilibrium equations are as follows:

$$\frac{dF}{dz} + 2\pi r_i \tau_i = 0 \tag{1}$$

$$\frac{dF}{dz} + 2\pi r_m \tau_m = 0 (2)$$

From equations (1) and (2), we have:

$$\tau_i r_i = r_m \tau_m = r \tau \tag{3}$$

where

F = fiber force at z

 r_f , r = radius of fiber and interphase, respectively

 τ_i , τ_m = shear stress of interphase and matrix, respectively.

From the theory of elasticity and Figure 4:

$$\tau = \frac{dW}{dr}G$$

$$r_F \le r \le r_i$$

$$\frac{dW}{dr} = \frac{\tau}{G_i} \tag{4}$$

where τ is the shear stress in the interphase, and G_i is the shear modulus of interphase.

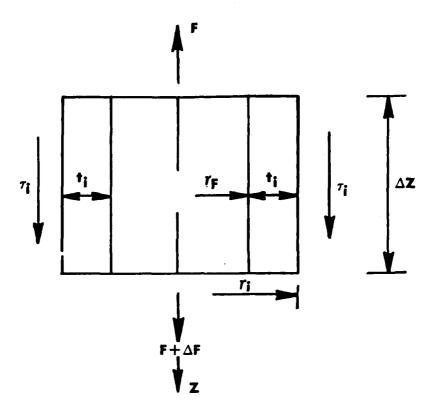


Figure 3a. Free Body Diagram Involving Fiber and Interphase.

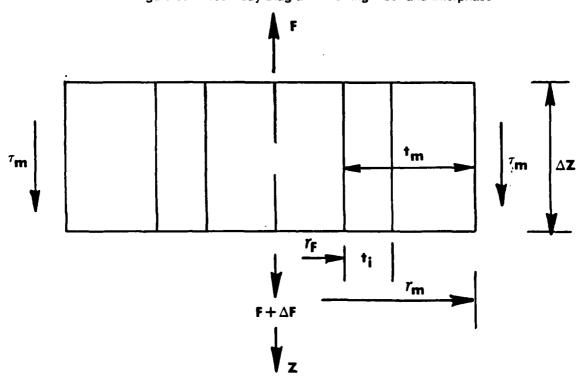


Figure 3b. Free Body Diagram Involving Fiber, Interphase, and Matrix.

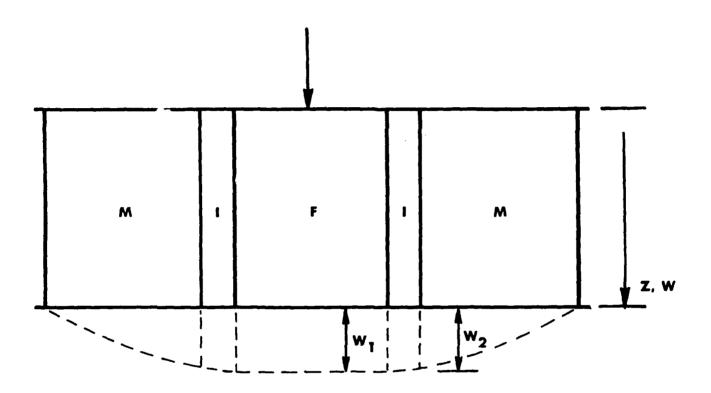


Figure 4. Axial Displacement of Fiber, Interphase, and Matrix.

From equation (3):

$$\tau = \frac{\tau_i r_i}{r} \tag{5}$$

substituting equation (5) into (4) and integrating, we have:

$$w = \frac{\tau_i r_i}{G_i} \ln(r) + C \tag{6}$$

but,

at
$$r = r_f$$
, $w = w_1$

$$r = r_{l_*} \quad w = w_2$$

Applying these boundary conditions to equation (6), we have:

$$\tau_i = \frac{(w_2 - w_1)G_i}{r_i \ln\left(\frac{r_i}{r_f}\right)} \tag{7}$$

By the same procedure and noting that at $r=r_m$, w=0 we have:

$$\tau_m = \frac{-w_2 G_m}{r_m \ln{(\frac{r_m}{r_i})}} \tag{8}$$

Also,

$$F = E_f \pi r_f^2 \frac{d w_1}{dz} \tag{9}$$

substituting equations (7) through (9) into equation (1) and (2) we have:

$$\frac{d^2w_1}{dz^2} - \frac{2G_i}{E_f r_f^2 ln\left(\frac{r_i}{r_f}\right)} (w_{1-}w_2) = 0$$
 (10)

$$\frac{d^2w_1}{dz^2} - \frac{2G_m}{r_f^2 E_f \ln{(\frac{r_m}{r_i})}} w_2 = 0$$
 (11)

After some algebraic manipulations of equations (10) and (11), we have:

$$\frac{d^2w_1}{dz^2} - \alpha^2 w_1 = 0 ag{12}$$

where

$$\alpha^{2} = \frac{\frac{2G_{i}}{E_{f} r_{f}^{2} ln\left(\frac{r_{i}}{r_{f}}\right)}}{\frac{G_{i} ln\left(\frac{r_{m}}{r_{i}}\right)}{G_{m} ln\left(\frac{r_{i}}{r_{f}}\right)}}$$

The solution of equation (12) is:

$$w_1 = C_1 \cosh(\alpha z) + C_2 \sinh(\alpha z) \tag{13}$$

since

$$z = 0, \quad F = -P_0 = -\pi r_f^2 \overline{\sigma} = E_f \pi r_f^2 \frac{dw_1}{dz}$$

$$z = l, \quad w_1 = 0 \tag{14}$$

where $\bar{\sigma}$ is the average applied stress at the fiber end.

Applying the boundary conditions (i.e., equation (14)) to equation (13), we have:

$$w_1 = -\frac{\overline{\sigma}}{E_f \alpha} (-\tanh(\alpha l) \cosh(\alpha z) + \sinh(\alpha z))$$
 (15)

 w_2 is obtained from equations (11) and (15) such that:

$$w_2 = \frac{r_F^2 E_F \alpha^2 \ln\left(\frac{r_m}{r_i}\right)}{2G_m} w_1 \tag{16}$$

From equations (7), (15), and (16), the interphase shear stress at $r=r_i$ is written as:

$$\tau_{i} = \frac{\overline{\sigma}\sqrt{G_{m}}}{\sqrt{2E_{f}}} \frac{r_{f}}{r_{i}} \frac{(-\tanh(\alpha l)\cosh(\alpha z) + \sinh(\alpha z))}{\sqrt{\frac{G_{m}}{G_{i}}\ln(\frac{r_{i}}{r_{f}}) + \ln(\frac{r_{m}}{r_{i}})}}$$
(17)

From equation (3), the interphase shear stress at $r=r_f$ is written as:

$$\overline{\tau_i} = \frac{\overline{\sigma}}{\sqrt{2}} \sqrt{\frac{G_m}{E_f}} \frac{(-\tanh(\alpha l)\cosh(\alpha z) + \sinh(\alpha z))}{\sqrt{\frac{G_m}{G_i} \ln(\frac{r_i}{r_f}) + \ln(\frac{r_m}{r_i})}}$$
(18)

The maximum interphase shear stress occurs at:

$$\tau_{\max} = (\overline{\tau_i})_{z=0} = -\frac{\overline{\sigma}}{\sqrt{2}} \sqrt{\frac{G_m}{E_f}} \frac{\tanh(\alpha l)}{\sqrt{\frac{G_m}{G_i} \ln(\frac{r_i}{r_f}) + \ln(\frac{r_m}{r_i})}}$$
(19)

Note that equation (19) contains two unknowns to be determined (namely, G, and r_i).

CORRELATION WITH MANDELL'S MICRODEBONDING TESTS

DETERMINATION OF INTERPHASE PROPERTIES

We now postulate that debonding of fiber from the matrix is due to interphase shear failure. Based on this assumption, the debonding criterion for the fiber/matrix interface is written as follows:

$$\tau_0 = \frac{\overline{\sigma_0}}{\sqrt{2}} \sqrt{\frac{G_m}{E_f}} \frac{\tanh(\alpha l)}{\sqrt{\frac{G_m}{G_i} \ln(\frac{r_i}{r_f}) + \ln(\frac{r_m}{r_i})}}$$
(20)

where

 τ_0 = interphase shear strength

 $\bar{\sigma}_0$ = average applied stress at the fiber end which causes fiber-matrix debonding (referred to as the debonding stress).

Let

$$r_i = r_f + t_i$$

$$r_m = r_f + t_m$$

where t_i is interphase thickness and t_m is the thickness combining interphase and matrix.

Equation (20) becomes:

$$\tau_0 = \frac{\overline{\sigma_0}}{\sqrt{2}} \sqrt{\frac{G_m}{E_f}} \frac{\tanh(\alpha l)}{\sqrt{\left(\frac{G_m}{G_i} - 1\right) \ln\left(1 + \frac{2t_i}{d_f}\right) + \ln\left(1 + \frac{2t_m}{d_f}\right)}}$$
(21)

From equation (21) we conclude that:

$$\frac{\overline{\sigma_0} tanh(\alpha l)}{\sqrt{\left(\frac{G_m}{G_i} - 1\right)ln\left(1 + \frac{2t_i}{d_f}\right) + ln\left(1 + 2\frac{t_m}{d_f}\right)}} = constant \tag{22}$$

By selecting $t_m/d_t = 0.4$ and $t_m/d_t = 1.0$ to correlate the test data,¹ the following results were obtained (for detailed calculations, refer to Appendix A).

For S-glass/epoxy,

$$\left(\frac{G_m}{G_i} - 1\right) \ln\left(1 + \frac{2t_i}{d_f}\right) = 1.8446$$

$$\tau_0 = 39 \ MPa$$
(23)

For graphite/epoxy

$$\left(\frac{G_m}{G_i} - 1\right) \ln\left(1 + \frac{2t_i}{d_f}\right) = 2.0672$$

$$\tau_0 = 27 \ MPa$$
(24)

Note that G_i and t_i cannot be determined separately from equations (23 and (24), but if t_i can be determined from an experiment, then G_i can be determined. Tables 1 and 2 list the interphase properties of S-glass/epoxy and graphite/epoxy, respectively, for various interphase thickness values and show the interphase shear modulus to be softer than bulk matrix for both S-glass/epoxy and graphite/epoxy composite materials.

CORRELATION WITH MICRODEBONDING TEST RESULTS

After the interphase shear strength has been determined, the debonding stress $\bar{\sigma}_0$ is determined as follows:

$$\overline{\sigma_0} = \sqrt{2}\tau_0 \sqrt{\frac{E_f}{G_m}} \sqrt{\frac{G_m}{G_i} - 1) \ln(1 + \frac{2t_i}{d_f}) + \ln(1 + \frac{2t_m}{d_f})}$$
 (25)

Making use of equations (23) and (24), and noted that we have for S-glass/epoxy:

$$\overline{\sigma_0} = \tau_0 \sqrt{2 \frac{E_f}{G_m}} \sqrt{1.8446 + \ln(1 + \frac{2t_m}{d_f})}$$
 (26)

and for graphite/epoxy:

$$\overline{\sigma_0} = \tau_0 \sqrt{2 \frac{E_f}{G_m}} \sqrt{(2.0672 + \ln(1 + \frac{2t_m}{d_f}))}$$
(27)

Equations (26) and (27) are plotted in Figures 5 and 6. The correlations with the microdebonding test results are excellent.

Table 1. Interphase Properties of S-glass Epoxy

Interphase Shear Strength = 39 MPA

ti/df	tį (nm)	G _m /G _i
.001	10	922
.005	50	184
.01	100	92
.05	500	18
.1	1000	9.0

Table 2. Interphase Properties of Graphite/Epoxy

Interphase Shear Strength = 27 MPA

t;/d;	t; (nm)	G _m /G _i
.0014	10	724
.0071	50	145
.0143	100	74
.0714	500	15
.143	1000	7

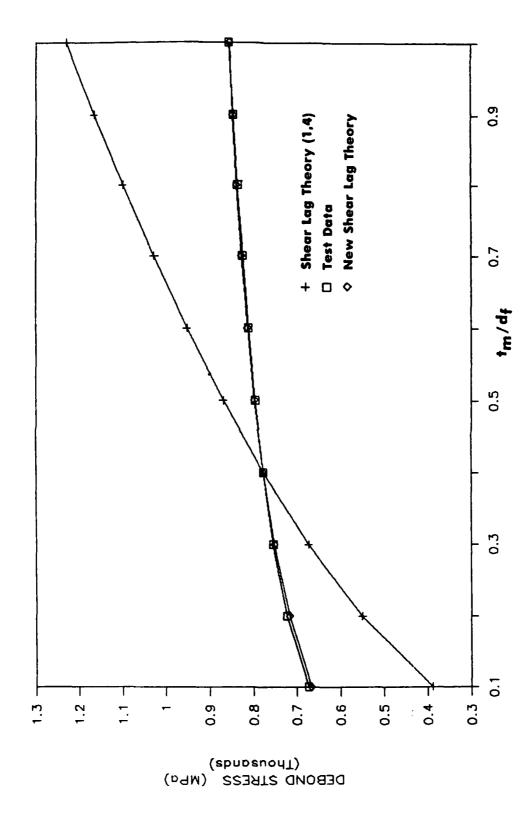


Figure 5. Variation of Debond Stress vs. t_m/d_f for S-glass/Epoxy.

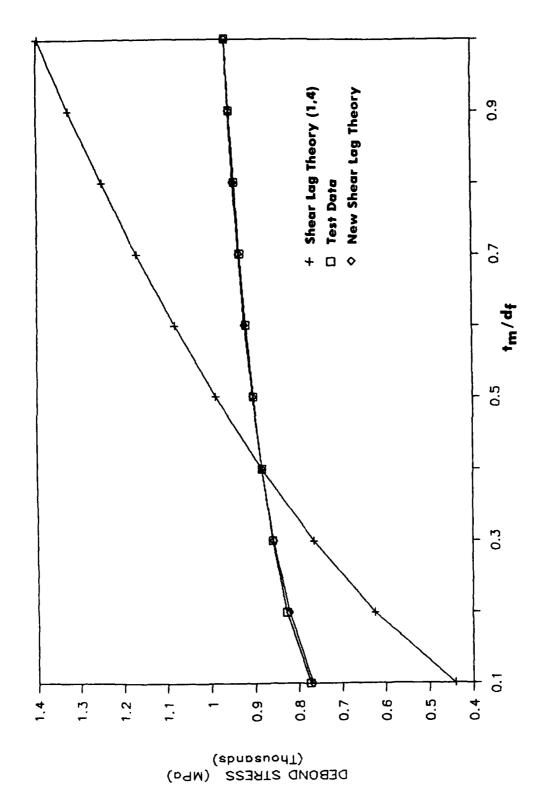


Figure 6. Variation of Debond Stress vs. t_m/d_f for Graphite/Epoxy.

INFLUENCE OF INTERPHASE PROPERTIES ON INTERPHASE SHEAR AND FRACTURE TOUGHNESS OF COMPOSITES

INTERPHASE SHEAR STRESS

Equation (19) can be rewritten as:

$$\frac{\tau_{\text{max}}}{\overline{\sigma}} = \frac{-1}{\sqrt{2}} \sqrt{\frac{G_m}{E_f}} \frac{1}{\sqrt{(\frac{G_m}{G_i} - 1) \ln(1 + \frac{2t_i}{d_f}) + \ln(1 + \frac{2t_m}{d_f})}}$$
(28)

Let

$$K_{\rm s} = ({\rm stress\ concentration\ factor}) = \frac{1\tau_{\rm max}1}{\overline{\sigma}} \sqrt{\frac{E_f}{G_m}}$$
 (29)

Thus

$$K_{s} = \frac{1}{\sqrt{2}} \frac{1}{\sqrt{\frac{G_{m}}{G_{i}} - 1) \ln(1 + \frac{2t_{i}}{d_{f}}) + \ln(1 + \frac{2t_{m}}{d_{f}})}}$$
(30)

Equation (30) is plotted in Figures 7 and 8 for K_s vs. G_m/G_i for various ratios. We can conclude that:

- (1) The lower the G_m/G_i ratio, the higher the stress concentration and the more likely debonding.
- (2) The thinner the interphase thickness, t_i , the higher the stress concentration, again making debonding easier.

MODE I FRACTURE TOUGHNESS

Murphy,³ etc., showed that the Mode I fracture energy of unidirectional composites can be expressed as follows:

$$(G_I)_c = (1 - v_f)G_M + v_f(G_F + G_{INF})$$
 (31)

where

 $(G_i)_c$ = Mode I fracture energy of composite

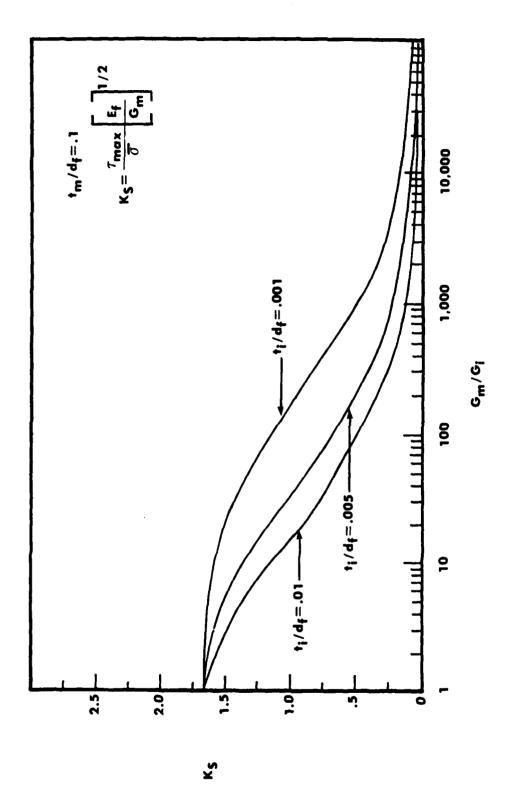


Figure 7. Effect of Interphase Shear Modulus on Maximum Stress for $t_{\rm m}/d_{\rm f}=0.1$.

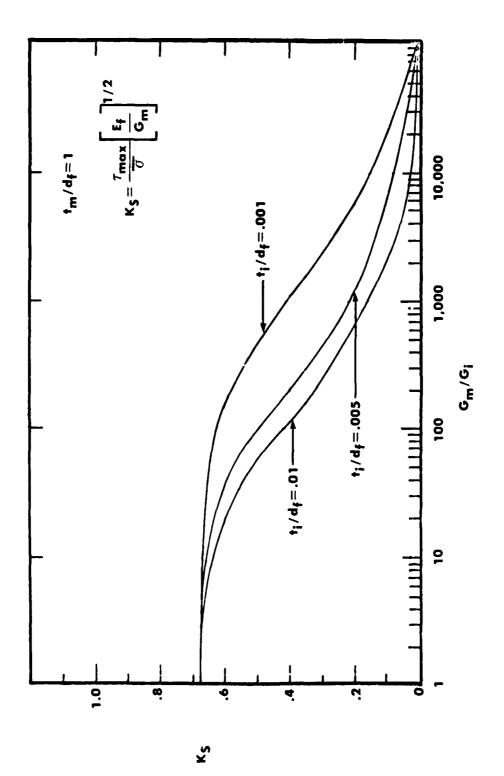


Figure 8. Effect of Interphase Shear Modulus on Maximum Interfacial Shear Stress for $t_m/d_f = 1.0$.

 G_{M} = Mode I fracture energy of matrix

G_F = Mode I fracture energy of fiber

 v_f = volume fraction of fiber

 G_{INF} = Mode I fracture energy associated with the decohesion of the fiber matrix interface.

Murphy further showed that:

$$G_{INF} = \frac{d_f \, \sigma_{fu}^3}{4\tau_f E_f} (1 - g + g^2 - g^3 + \frac{1}{2} (\frac{l_p}{l_d})^2 (\frac{E_f}{\sigma_{fu}}) (1 - g)^2) \tag{32}$$

where

 σ_{f_u} = ultimate stress of fiber

 $I_d = (d_f/4\tau_f) (\sigma_{fu} - \bar{\sigma}_0)$

 $\bar{\sigma}_{c}$ = debonding stress

I_p ≈ fiber pull-out length

 τ_f = post debonding friction shear stress

$$g = \frac{\overline{\sigma_0}}{\sigma_{fu}} = \text{debonding fracture ratio}$$
(33)

Examining equations (31) and (32), it can be seen that the smaller the g (i.e., weaker interface), the larger the G_{INF} and hence, the tougher the composite. On the other hand, the larger, the g (i.e., stronger interface), the smaller the G_{INF} yielding a more brittle composite. If g=1, (i.e., the fiber breaks with no debonding between fiber and matrix), equation (31) reduces to:

$$(G_I)_c = (1-V_f) G_M + V_f G_F$$

Murphy³ showed that for high-volume fractions the Mode I fracture energy, $(G_i)_c$, of composites can range over five orders of magnitude, while the debonding fracture ratio, g, ranges from zero to one.

From equations (29) and (33), g can be expressed as follows:

$$g = \frac{\tau_0}{\sigma_{fu}} \frac{1}{K_s} \sqrt{\frac{E_f}{G_m}} \tag{34}$$

To demonstrate how interphase properties will effect the Mode I fracture toughness of the composite, equation (32) is rewritten as follows:

$$\frac{G_{INF}}{C_{INF}} = 1 - g + g^2 - g^3 + \frac{1}{2} (\frac{l_p}{l_d})^2 (1 - g)^2$$
(35)

where

$$C_{INF} = \frac{d_f \sigma_{fu}^3}{4\tau_f E_f}$$

For simplicity, assume $l_p = 0$ (i.e., no fiber pull-out occurs during fracture of composite). Equation (35) then becomes:

$$\frac{G_{INF}}{C_{INF}} = 1 - g + g^2 - g^3 \tag{36}$$

Assuming that the interphase strength, τ_0 , is constant for various interphase thicknesses and making use of equation (34), equation (36) is plotted as shown in Figures 9 and 10. The detailed calculation is shown in Appendix B.

From the plots, it can be seen that when the interphase property, G_{in} , is closer to the bulk matrix, G_{in} , the composite material will have higher fracture toughness. Note that the thinner the interphase thickness, t_{in} , the tougher the composite material.

FINITE ELEMENT SIMULATION

MICRODEBONDING PROBLEM

An axisymmetric finite element model that includes the interphase was developed. Interphase properties were obtained by either using the values contained in Tables 1 and 2 or those derived from using equation (23) for S-glass/epoxy and equation (24) for graphite/epoxy for various interphase thicknesses. Only those results for graphite/epoxy are presented. Figures 11 and 12 are typical models used to analyze the microdebonding problem. The NASTRAN computer code was used to perform the analysis. Note that the top surface and side surface corresponding to outside radius were assumed fixed. A 1 N force was applied at the center of the cylindrical composite disc.

Figure 13 shows the typical interphase shear distribution along the axis. The maximum shear stress occurs at approximately 0.4 fiber diameter below the surface. Shear lag theory positions the maximum shear at the surface. Note that the magnitude of the interface shear for composite without an interphase (i.e., $G_m/G_i = 1.0$) is much higher than for a composite with an interphase. This result agrees with the conclusion from the shear lag analysis in the foregoing section.

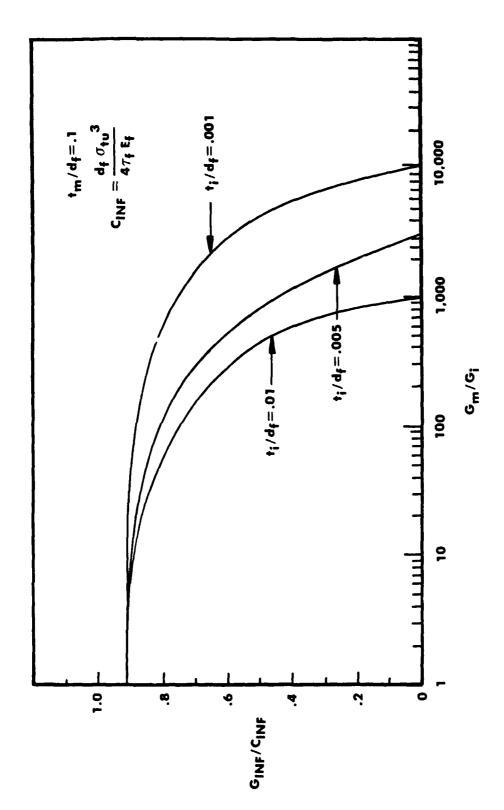


Figure 9. Effect of Interphase on Opening Mode Fracture Energy of a Unidirectional Fiber Composite for $t_{\rm m}/d_{\rm f}=0.1$.

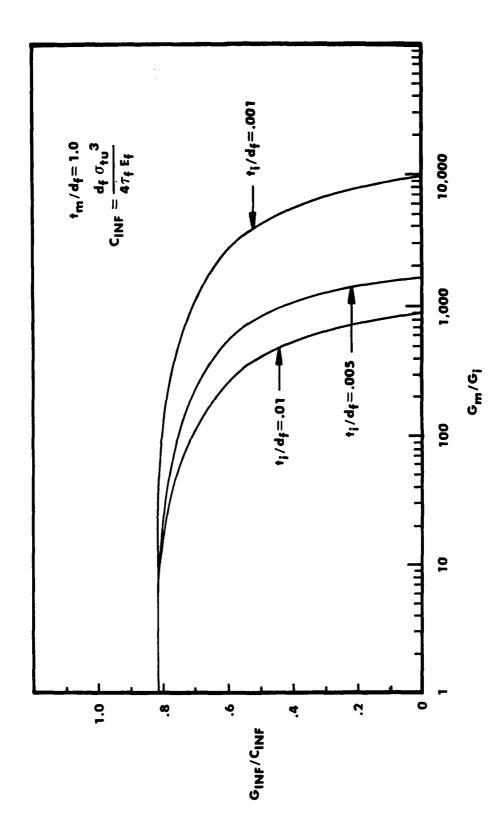


Figure 10. Effect of Interphase on Opening Mode Fracture Energy of a Unidirectional Fiber Composite for $t_m/d_f = 1.0$

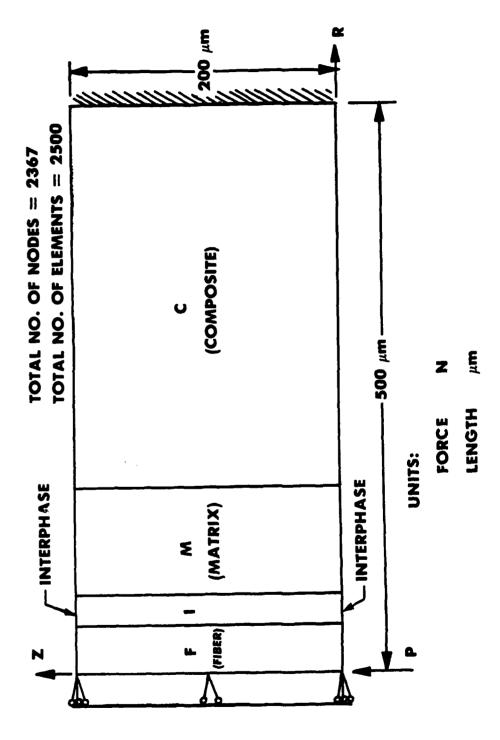


Figure 11. Finite Element Model for Axisymmetric Solid.

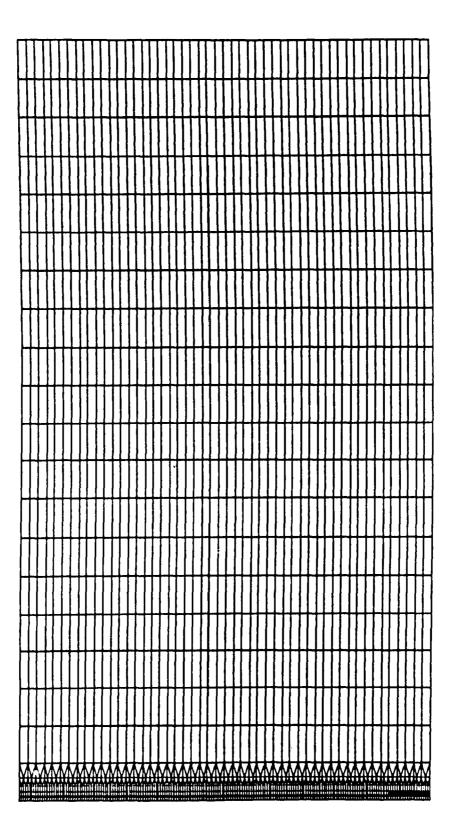


Figure 12. Axisymmetric Finite Element Model for Microdebonding Problem.

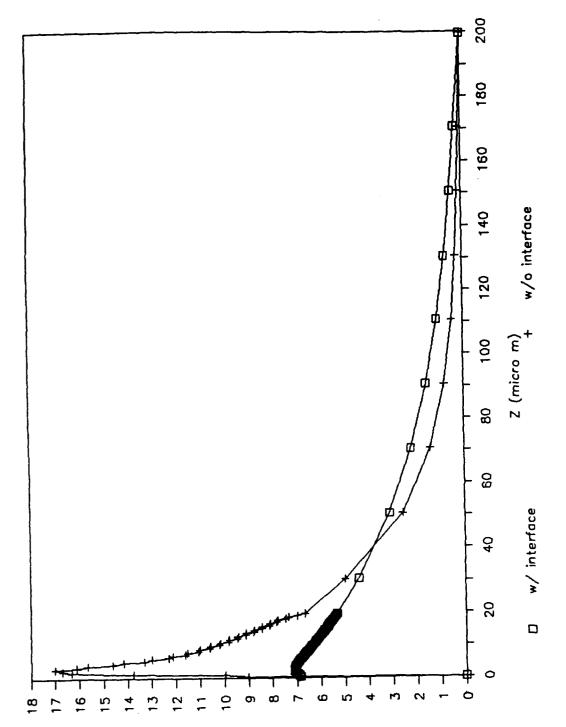


Figure 13. Interphase Effect on Interfacial Shear ($t_m/d_f=0.36$, $V_f=0.4$, $t_i=0.1~\mu m$).

interfacial shear dist.(N/micro m)X10-4

Figure 14 shows the prediction of debonding stress $\bar{\sigma}_0$, for $t_m/d_f = 0.1$ and $t_m/d_f = 1.0$, where data for $t_m/d_f = 0.4$ was used to determine the interphase shear strength. We see that the model, which includes the interphase, provides a better solution than those without the interphase.

Also, note that interphase shear strength predicted by finite element analysis, 23.9 mpa, is close to that predicted by the shear lag theory. (For detailed calculation, refer to Appendix A. This interphase shear strength value is different from the values of interfacial shear strength obtained by other investigators.¹

Figure 15 shows the fiber end displacement in the axial direction under a 1.0 N axial load applied at the fiber end. The correlation between the finite element analysis and new shear lag theory is very good, validating the adequacy of the shear lag theory.

INTERPHASE EFFECT ON OUT-OF-PLANE DISPLACEMENT

Finite element calculations were performed to determine the effect of the interphase on the out-of-plane displacement using the model shown in Figure 16. This model corresponds to the experimental geometry used for tensioned fiber tests in reference 14. Figures 17 and 18 show the predicted out-of-plane displacements with and without interphase for $G_{\rm m}/G_{\rm i}$ =25 and $G_{\rm m}/G_{\rm i}$ =74 respectively. It can be seen that a significant displacement gradient occurs in the vicinity of interphase region. Thus, the interphase region may be defined as a region with a very high displacement gradient allowing the dimension of interphase to be determined through direct measurement of the length of this high displacement gradient region.

The results shown in Figures 17 and 18 were adjusted for a 0.4% fiber strain load and correlated with test results shown in Figure 19. Interphase properties with $G_{\rm m}/G_{\rm i}=25$ and $t_{\rm i}=0.1\mu{\rm m}$ match the test data. However, if this method is not believed adequate to determine the exact interphase thickness, then the radial displacement field must also be measured in addition to the axial displacement field so that the test results can be correlated to determine separate values for the interphase thickness and modulus. Note that the softer the interphase, the greater the displacement gradient in the interphase region.

DISCUSSION AND CONCLUSION

The ratio between interphase shear modulus and thickness can be established from shear lag analysis, but not specific values for G_i or T_i separately. If the interphase thickness can be determined from an experimental measurement, then equation (23) or equation (24) can be used to calculate the interphase shear modulus for S-glass/epoxy and graphite/epoxy, respectively. If the interphase thickness is not available experimentally, then an iteration procedure must be performed using equations (23) and (24) as starting values for interphase shear modulus and thickness. Iterate G_i and T_i until the analytical results (i.e., out-of-plane displacement and radial displacement) converge to the test results. More studies need to be pursued of this approach to compute G_i or T_i .

In this report it is assumed that the interphase is an axisymmetric region of uniform modulus and fixed radial dimension. We recognize that the true interphase region has radially varying properties and can also exhibit circumferential property gradients.

For a tougher composite, equation (32) and Figures 9 and 10 suggest that the composite material must possess:

- 1. Larger fiber diameter and fiber ultimate stress
- 2. Smaller post debond frictional shear stress and fiber Young's modulus
- 3. Smaller interphase shear strength
- 4. Smaller interphase thickness and G_m/G_i ratio.

Although interphase shear strength, τ_0 , and post debond frictional shear stress vary with interphase thickness, t_i , Figures 9 and 10 give approximate guidelines for obtaining tougher composite materials. Note that the weaker interface (i.e., small interphase shear strength) provides tougher fracture resistance, but may affect the strength of composite, especially short fiber composites.

The following conclusions are drawn from this study:

- 1. By including the interphase, both shear lag analysis and finite element analysis provide much better predictions of material response.
- 2. The interphase exists and is softer than the matrix for the composites used by Mandell in his microdebonding tests (i.e., S-glass/epoxy and graphite/epoxy).
- 3. The properties and thickness of the interphase have significant influence on the interface stress, displacement, and fracture toughness of fibrous composites.

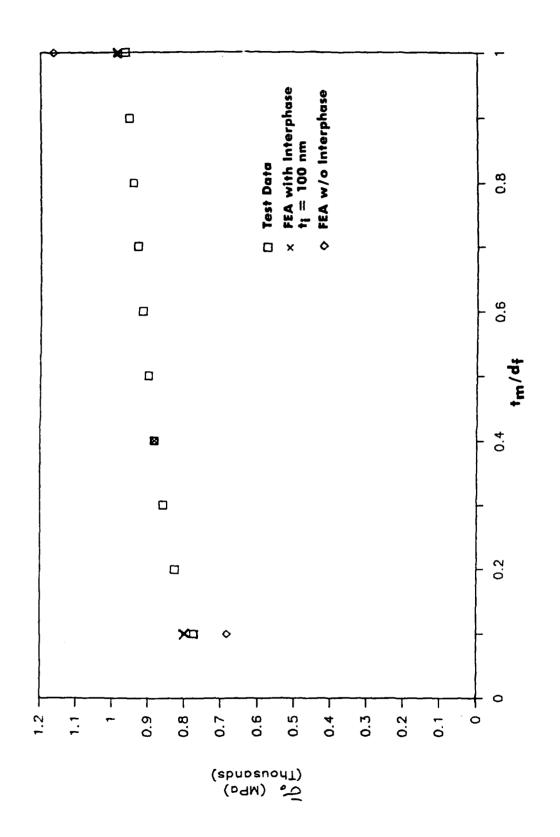


Figure 14. Variation of σ_0 vs. t_m/d_f as Predicted by FFEA With and Without Interphase for Graphite/Epoxy.

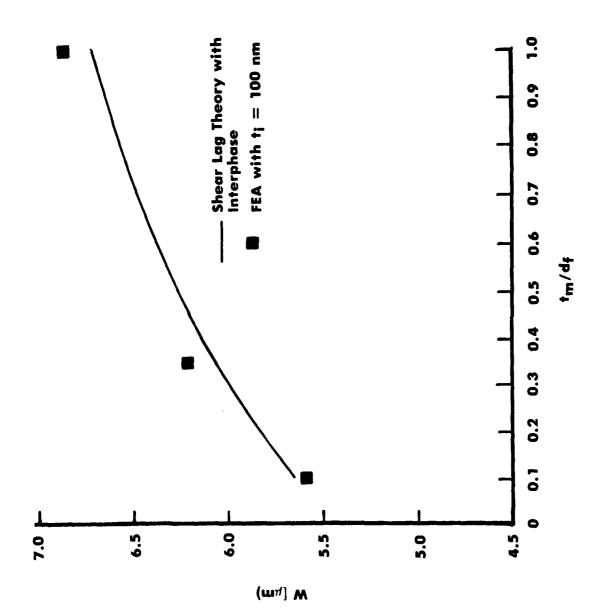


Figure 15. Axial Displacement of Fiber End Under 1 N Load Applied at Fiber End.

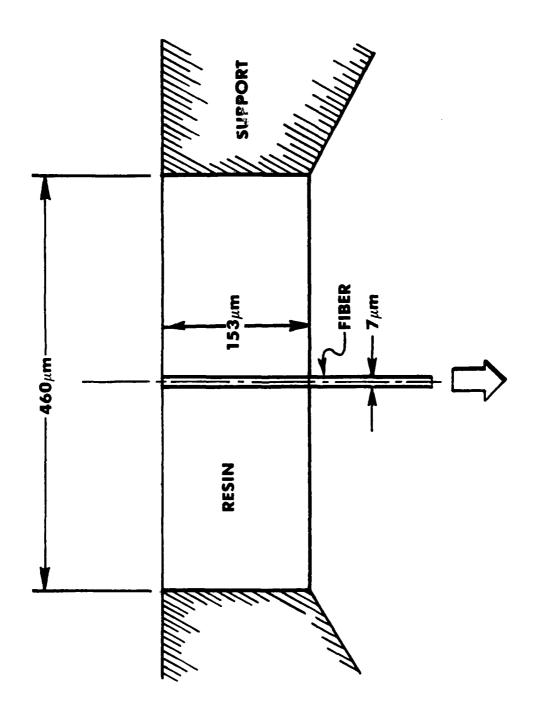
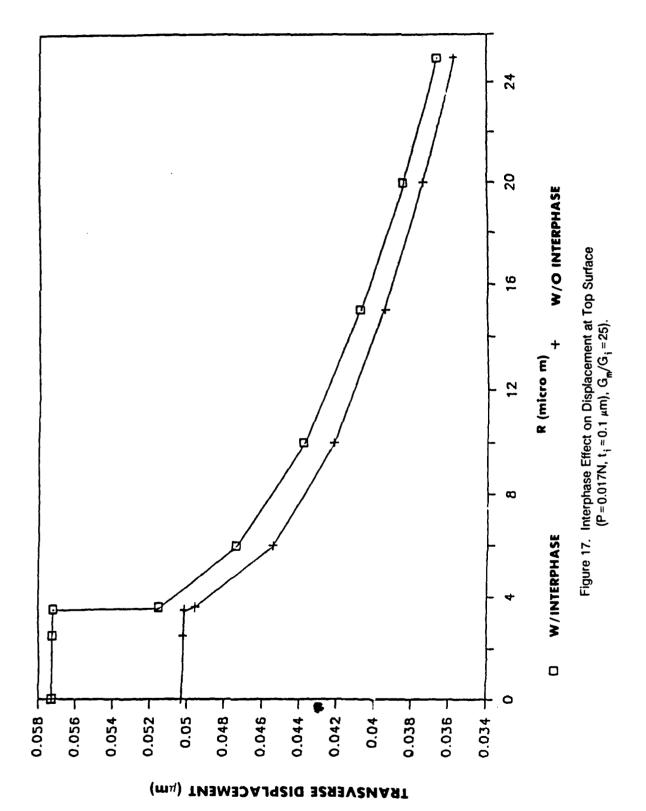


Figure 16. Modeling of Matrix Deformation Near Loaded Fiber.



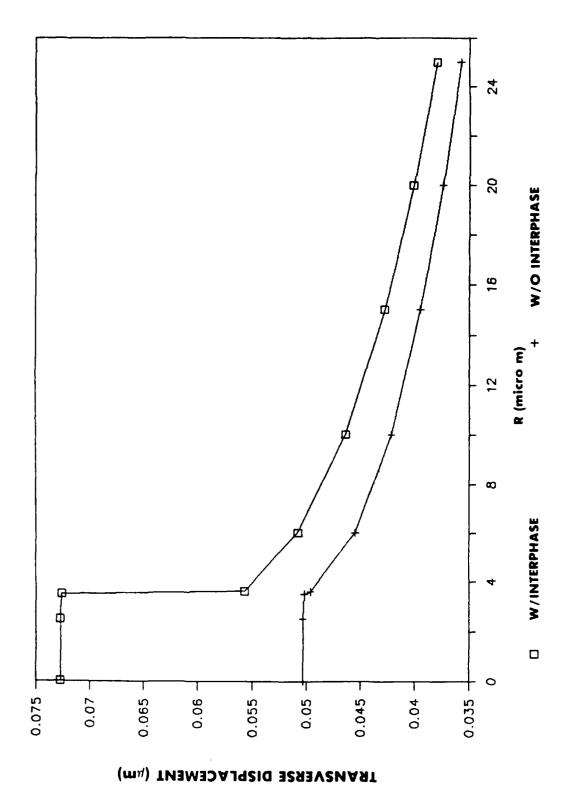


Figure 18. Interphase Effect on Displacement at Top Surface (P = -0.017N, $t_i = 0.1 \,\mu\text{m}$), $G_m/G_i = 74$).

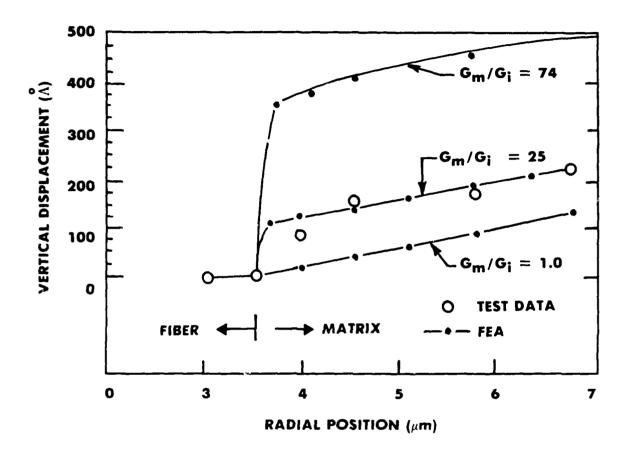


Figure 19. Correlation of Finite Element Analysis and Out-of-Plane Displacement Test Data for 0.4% Fiber Strain Load With t_i =0.1 μ m.

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APPENDIX A: DETERMINATION OF INTERPHASE PROPERTIES FOR S-GLASS/EPOXY AND GRAPHITE/EPOXY

NEW SHEAR LAG THEORY

INTERPHASE PROPERTIES

From equation (22), we have:

$$\frac{\overline{\sigma} \tanh(\alpha I)}{\left\{ \left(\frac{G_m}{G_I} - 1 \right) \ln \left(1 + \frac{2t_I}{d_f} \right) + \ln \left(1 + \frac{2t_m}{d_f} \right) \right\}^{1/2}} - Const$$
(A-1)

Substituting $t_{\rm m}/d_f$ = 1.0 and $t_{\rm m}/d_f$ = 0.4 into equation (A-1), and note that $t_{\rm m}/d_f$ = 1.0, we have:

$$\frac{\overline{\sigma_{1.0}}}{(A+1.0986)^{1/2}} = \frac{\overline{\sigma_{0.4}}}{(A+0.5878)^{1/2}}$$
 (A-2)

where

 $\bar{\sigma}_{0.4}$, $\bar{\sigma}_{1.0}$ = debonding stress of fiber/matrix interface corresponding to $t_{\rm m}/d_f$ = 1.0 and $t_{\rm m}/d_f$ = 0.4, respectively

$$A - \left(\frac{G_m}{G_i} - 1\right) \ln \left(1 + \frac{t_i}{r_i}\right) \tag{A-3}$$

Equation (A-2) can be rearranged as follows:

$$\left(\frac{G_m}{G_i} - 1\right) \ln\left(1 + \frac{t_i}{r_i}\right) - \frac{(1.0986 - 0.5878 \,\mathrm{B})}{(\mathrm{B} - 1)} \tag{A-4}$$

where

$$B = (\overline{\sigma}_{1,0}/\overline{\sigma}_{0,4})^2 \tag{A-5}$$

For S-glass/epoxy, from reference 1:

$$\frac{\overline{\sigma_{1,0}}}{\overline{\sigma_{0,4}}} - 1.1$$

equation (A-4) becomes:

$$\left(\frac{G_m}{G_l}-1\right)\ln\left(1+\frac{t_l}{r_l}\right)-1.8446$$

For graphite/epoxy, from reference 1:

$$\frac{\overline{\sigma_{1,0}}}{\overline{\sigma_{0,4}}}$$
 - 1,092

B-1.1924

equation (A-4) becomes:

$$\left(\frac{G_m}{G_i} - 1\right) \ln \left(1 + \frac{t_i}{r_i}\right) - 2.0672$$

INTERPHASE-SHEAR STRENGTH

From equation (28), the maximum interfacial shear stress can be written as follows:

$$\tau_{\text{max}} = \frac{\overline{\sigma}}{\sqrt{2}} \sqrt{\frac{G_m}{E_I}} \left\{ \left(\frac{G_m}{G_0} - 1 \right) \ln \left(1 + \frac{t_I}{t_I} \right) + \ln \left(1 + \frac{2t_m}{d_I} \right) \right\}^{-1/2}$$
(A-6)

For S-glass fiber $G_m = 1.07$ GPA, $E_f = 86$ GPA from reference 1, for $t_m/d_f = 0.4$, $\bar{\sigma} = 777$ MPA, equation (A-6) becomes:

$$\tau_0 = 39 \text{ MPA}$$

For G_r/G_p , $G_m=1.21$ GPA, $E_f=241$ GPA, from reference 1, for $t_m/d_f=0.4$, $\bar{\sigma}=883$ MPA, equation (A-6) becomes:

$$\tau_0 = 27 \text{ MPA}$$

OUT-OF-DISPLACEMENT OF FIBER

From shear lag theory, the fiber axial displacement at z=0 can be written as:

$$w - \frac{\overline{\sigma}}{E_t \alpha} \tag{A-7}$$

where

$$\alpha = \frac{\sqrt{2}}{r_f} \sqrt{\frac{G_m}{E_f}} \left\{ \left(\frac{G_m}{G_f} - 1 \right) \ln \left(\frac{r_f}{r_f} \right) + \ln \left(\frac{r_m}{r_f} \right) \right\}^{-1/2}$$
(A-8)

For graphite/epoxy an P=1 N, equation (A-7) becomes:

$$w - \frac{\overline{\sigma}}{E_t \alpha} - \frac{25.984}{241} \frac{1}{\alpha} - \frac{0.1078}{\alpha}$$
 (A-9)

$$\alpha = 0.0286 \left\{ 2.0672 + ln \left(1 + \frac{2 t_m}{d_t} \right) \right\}^{-1/2}$$
 (A-10)

DEBONDING STRESSES

Graphite/Epoxy

From equation (A-1), we have:

$$\frac{\overline{\sigma}}{\left\{2.0672 + \ln\left(1 + \frac{2t_m}{d_t}\right)\right\}^{-1/2}} = \frac{\sigma_{1.0}}{\left\{2.0672 + 1.0986\right\}^{1/2}}$$

After simplification, we have:

$$\bar{\sigma} = 542.36 \left\{ 2.0672 + \ln \left(1 + \frac{2t_m}{d_t} \right) \right\}^{1/2}$$

 σ vs. t_m/d_f is tabulated as shown in Table A-1.

S-glass/Epoxy

From equation (A-1) we have:

$$\frac{\overline{\sigma}}{\left\{1.8446 + \ln\left(1 + \frac{2t_m}{d_I}\right)\right\}^{1/2}} = \frac{\overline{\sigma}_{1.0}}{\left\{1.8446 + 1.0986\right\}^{1/2}}$$

After simplification we have:

$$\overline{\sigma}$$
 - 498.375 $\left\{1.8446 + \ln\left(1 + \frac{2t_m}{d_t}\right)\right\}^{1/2}$

 σ VS. $t_{\rm m}/d_{\rm f}$ is tabulated as shown in Table A-2.

Table A-1. $\bar{\sigma}$ vs. t_m/d_f for Graphite/Epoxy

t_m/d_f	o Test (MPA)	ō (MPA)	E _{./.}
0.1	773.6	813.45	5.2
0.2	826.8	840.86	1.7
0.3	859.7	863.9	0.49
0.4	883.0	883.0	0.
0.5	902.9	901.09	-0.2
0.6	918.8	916.51	-0.25
0.7	932.5	930.37	-0.23
8.0	944.5	942.94	-0.17
0.9	955.3	954.4	-0.09
1.0	965.0	96 5.0	0.

Table A-2. $\bar{\sigma}$ vs. t_m/d_f for S-glass/Epoxy.

t_m/d_t	ō Test (MPA)	ē (MPA)	E <u>./.</u>
0.1	673.0	709.5	5.4
0.2	723.0	736.0	1.8
0.3	754.0	758.2	.56
0.4	777.0	777.0	0.
0.5	795.5	793.92	-0.2
0.6	810.8	808.7	-0.26
0.7	823.9	821.95	-0.24
8.0	835.4	833.95	-0.17
0.9	845.7	844.92	-0.09
1.0	855.0	855.0	. 0.

FINITE ELEMENT ANALYSIS

From finite element analysis, for center fiber subjected to $\bar{\sigma}$ =25,984.0 MPA (i.e., P=1 N), the computer outputs for interfacial shear, τ , and out-of-plane displacement, w, are shown in Table A-3.

Table A-3. Finite Element Results for $P=1 N (t_i = .1 \mu m)$.

t _m /d _t	(<u>um)</u>	τ (MPA)	
0.10	5.62	775.0	
0.35	6.23	710.7	
1.0	6.86	641.0	

INTERPHASE SHEAR STRENGTH

Define the interphase shear stress at $\tilde{\sigma}$ =883 MPA, which corresponds to the debonding stress of composite with $t_{\rm m}/d_f$ =0.4 as interphase shear strength, then τ_0 =704/25984×883=23.9 MPA.

DEBONDING STRESS $\bar{\sigma}$ vs. t_m/d_f

The debonding stress of composite for various t_m/d_f can be written as follows:

$$\frac{1}{\sigma} = \frac{25984}{\tau^*} \times 23.9$$
 (A-11)

where

 τ^* = computer output of interphase shear stress corresponding to $\bar{\sigma}$ =25984 MPA.

Making use of data from Table A-3, we have the comparison of finite element results with the test results as shown in Table A-4.

Table A-4. Comparison of Debonding Stress Between Test and Finite Element Analysis.

t _m /d _t	σ̄ _{τest} (MPA)	τ * (MPA)	<i>ō</i> <u>MPA</u>
0.1	773.6	775.0	801.3
0.35	874.2	710.7	874.2
1.0	965.0	641.0	969.2

OUT-OF-PLANE DISPLACEMENT

The comparison of out-of-phase displacement for shear lag theory and finite element analysis is shown in Table A-5. Shear lag solution is based on equations (A-9) and (A-10).

Table A-5. Comparison of Out-of-Plane Displacement Between Shear Lag Theory and Finite Element Analysis.

t _m /d _f	w(μm) SHEAR _LAG_	w(μm) <u>F.E.A.</u>
0.1	5.653	5.62
0.2	5.84	_
0.3	6.004	-
0.4	6.075	6.23
0.5	6.2623	_
0.6	6.37	-
0.7	6.47	-
0.8	6.55	_
0.9	6.63	_
1.0	6.71	6.86

APPENDIX B: CALCULATION OF INTERPHASE SHEAR STRESS CONCENTRATION FACTOR AND MODE I FRACTURE ENERGY OF UNIDIRECTIONAL COMPOSITES

INTERPHASE SHEAR STRESS CONCENTRATION FACTOR, Ks

From equation (30) we have:

$$K_{s} = \frac{1}{\sqrt{2}} \frac{1}{\left\{ \left(\frac{G_{m}}{G_{l}} - 1 \right) \ln \left(1 + \frac{2t_{l}}{d_{l}} \right) + \ln \left(1 + \frac{2t_{m}}{d_{l}} \right) \right\}^{1/2}}$$
(B-1)

Equation (B-1) is used to calculate K_s for $t_m/d_t=0.1$ and $t_m/d_t=1.0$, respectively, as tabulated in Tables B-1 and B-2.

Table B-1. K_s vs. G_m/G_i for Various t_i/d_i $(t_m/d_i=0.1)$.

	K,					
G_m/G_i	$t_i/d_f = 0.001$	$t_i/d_f = 0.005$	$t_i/d_t = 0.01$			
1	1.66	1.66	1.66			
10	1.58	1.36	1.17			
10 ²	1.15	0.65	0.48			
10 ³	0.48	0.22	0.16			
104	0.16	0.1	0.05			
10 ⁵	0.05	0.02	0.02			

Table B-2. K_a vs. G_m/G_i for Various t_i/d_i $(t_m/d_i=1.0)$.

		r _s	
G_m/G_i	$t_i/d_f = 0.001$	$t_i/d_f = 0.005$	$t_1/d_1 = 0.01$
1	0.675	0.675	0.675
10	0.669	0.649	0.626
10 ²	0.621	0.49	0.404
10 ³	0.402	0.21	0.155
104	0.15	0.07	0.05
10 ⁵	0.05	0.02	0.02

MODE 1 FRACTURE ENERGY OF UNIDIRECTIONAL COMPOSITE

From equation (29):

$$\overline{\sigma} = \frac{|\tau_{\text{max}}|}{K_s} \left\{ \frac{E_f}{G_m} \right\}^{1/2}$$
 (B-2)

The debonding stress of fiber/matrix interface can be written as follows:

$$\overline{\sigma} = \frac{\tau_0}{K_s} \left\{ \frac{E_f}{G_m} \right\}^{1/2} \tag{B-3}$$

From equation (33):

$$g - \frac{\overline{\sigma_0}}{\sigma_{fi}} - \frac{\tau_0}{\sigma_{fi}K_s} \left\{ \frac{E_f}{G_m} \right\}^{1/2}$$
 (B-4)

For graphite/epoxy:

$$g = \frac{0.027}{2.5 K_s} \left\{ \frac{241}{1.21} \right\}^{1/2} = \frac{0.1524}{K_s}$$
 (B-5)

where $K_{\rm s}$ can be obtained from equation (B-1) and Tables B-1 and B-2.

Table B-3. G_{INF}/C_{INF} vs. G_m/G_i for Various t_i/d_f $(t_m/d_f=0.1)$.

	$t_i/d_f = 0.001$			t _i /d	$t_i/d_f = 0.005$			$t_i/d_i = 0.01$	
G_{n}/G_{i}	g	$1-g+g^2-g^3$	G_m/G_i	g	1-g+g²-g³	G _m /G	9	1-g+g2-g ³	
1	0.092	0.9157	1	0.092	0.9157	1	0.092	0.9157	
10	0.0965	0.912	10	0.112	0.90	10	0.1303	0.885	
10²	0.1325	0.883	10²	0.235	0.810	10²	0.3175	0.751	
10 ³	0.3175	0.751	10 ³	0.693	0.455	10 ³	0.9526	0.09	
104	0.9526	0.09	2130	1.0	0.	1078	1.0	0.	
10680	1.0	0.							

Table B-4. G_{INF}/C_{INF} vs. G_{m}/G_{i} for Various t_{i}/d_{f} (t_{m}/d_{f} = 1.0).

	t _i /d _t =0.001			t _i /d	$t_i/d_f = 0.005$			$t_i/d_f = 0.01$	
G_m/G_i	<u>g</u>	1-g+g²-g³	G_m/G_i	<u>g</u>	1-g+g2-g3	G_{m}/G_{i}	<u>g</u>	1-g+g2-g3	
1	0.2258	0.8137	1	0.2258	0.8137	1	0.2258	0.8137	
10	0.2278	0.8123	10	0.2348	0.8074	10	0.2435	0.8014	
10 ²	0.2454	0.800	10 ²	0.311	0.756	10 ²	0.3772	0.7114	
10 ³	0.3791	0.71	10 ³	0.72	0.425	10 ³	0.98	0.	
104	1.0	0.	2043	1.0	0.	1032	1.0	0.	

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